The Universe before the Hot Epoch

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Basic properties of the present Universe:

Visible Universe is large

Size of the visible part of the Universe is 15 Gigaparsec ≈ 45 billion light years

1 Mpc = $3 \cdot 10^6$ light yrs = $3 \cdot 10^{24}$ cm

The Universe is old

Its lifetime is at least 13.8 billion years

✓ Visible Universe is homogeneous on large scales ($\gtrsim 200$ Mpc): different parts of the Universe look the same.

Deep surveys of galaxies and quasars \implies map of a good part of visible Universe

The Universe expands

Space stretches out. Distances between galaxies increase in time.

Wavelength of a photon also increases.

If emitted at time t with wavelength λ , it comes to us with longer wavelength

 $\lambda_0 = (1+z)\lambda$

z = z(t): redshift, directly measurable.

3d space is Euclidean (observational fact!)
 Sum of angles of a triangle = 180°, even for triangles as large as the size of the visible Universe.

Qualification: curvature radius > $7 \times$ (radius of visible part)

NB: Di Valentino, Melchiorri, Silk, Nov. 2019, claim that spatial curvature is non-zero. Too premature, likely systematic effects. All above is encoded in space-time metric (Friedmann-Lemâitre-Robertson-Walker)

 $ds^2 = dt^2 - a^2(t)d\vec{x}^2$

 \boldsymbol{x} : comoving coordinates, label distant galaxies.

a(t)dx: physical distances.

a(t): scale factor, grows in time. Set its present value to 1, then a < 1 in the past.

$$1 + z(t) = 1/a(t)$$

 $H(t) = \frac{\dot{a}}{a}$: Hubble parameter, expansion rate

Present value

$$H_0 = (67.7 \pm 0.4) \ \frac{\mathrm{km/s}}{\mathrm{Mpc}} = (14 \cdot 10^9 \ \mathrm{yrs})^{-1}$$

(matter of some debate)

The Universe is warm. It is filled with Cosmis Microwave Background: photons that were thermally produced when the Universe was young and hot.

CMB temperature today

 $T_0 = 2.7255 \pm 0.0006$ K

Fig.

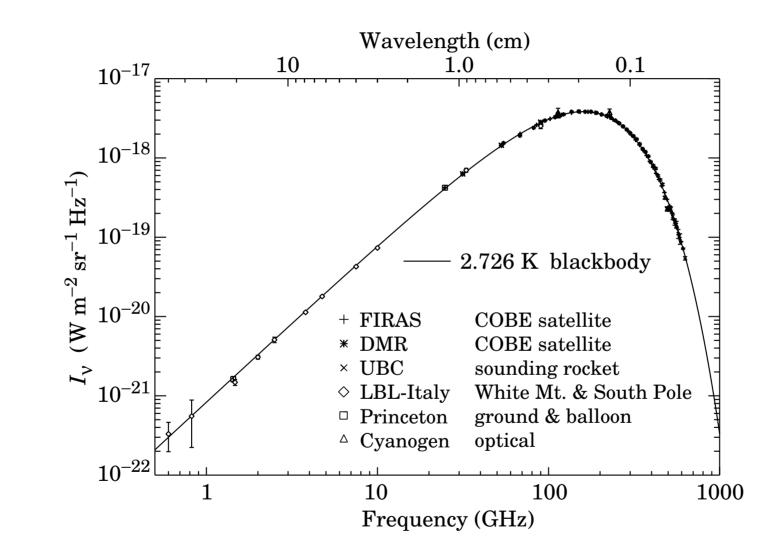
It was denser and warmer at early times.

It also expanded a lot faster at early times: according to General Relativity, expansion rate is determined by Friedmann equation

$$H^2 = \frac{8\pi}{3}G\rho$$

where ρ is energy density, G is Newton's gravity constant, $\hbar = c = k_B = 1$

CMB spectrum



T = 2.726 K

Cornerstones of thermal history

P Recombination, transition from plasma to gas.

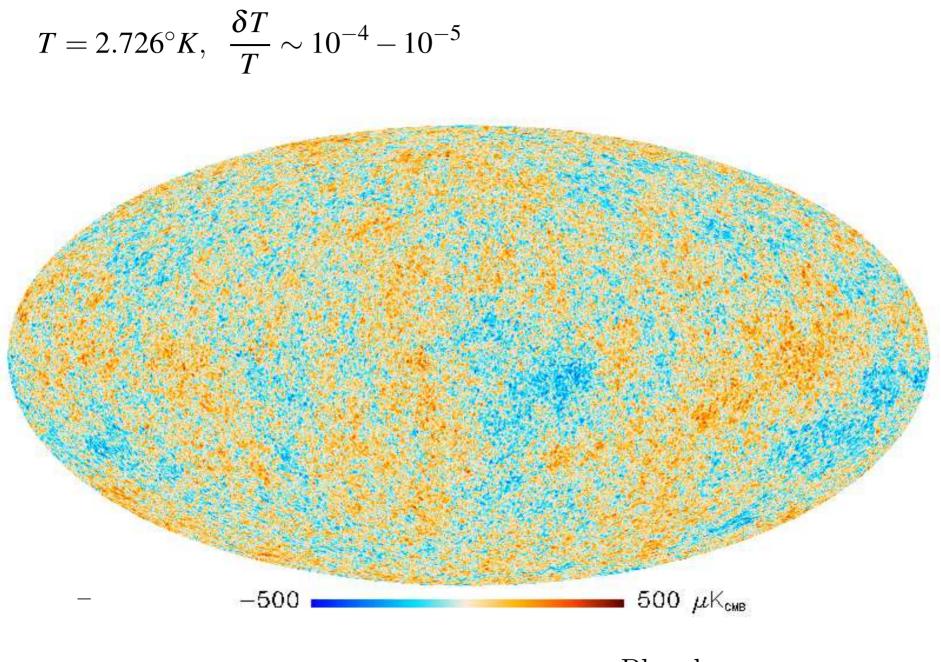
 $z = 1090, T = 3000 \text{ K}, t = 380\ 000 \text{ years}$

Last scattering of CMB photons

Photographic picture (literally!) of the Universe at that epoch Fig.

The Universe was much more homogeneous: the inhomogeneities were at the level

$$\frac{\delta\rho}{\rho} \sim 10^{-4} - 10^{-5}$$



Planck

D Big Bang Nucleosynthesis, epoch of thermonuclear reactions

$$p+n \rightarrow {}^{2}H$$

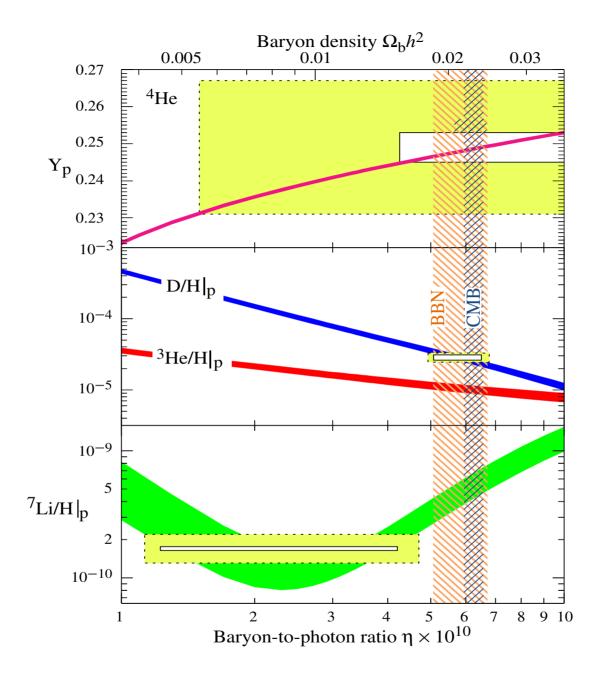
 ${}^{2}H+p \rightarrow {}^{3}He$
 ${}^{3}He+n \rightarrow {}^{4}He$
up to ${}^{7}Li$

Abundances of light elements: measurements vs theory

$$T = 10^{10} \to 10^9 \text{ K}, \quad t = 1 \to 500 \text{ s}$$

Fig.

Agreement between independent determinations of baryon content: BBN vs CMB anisotropy



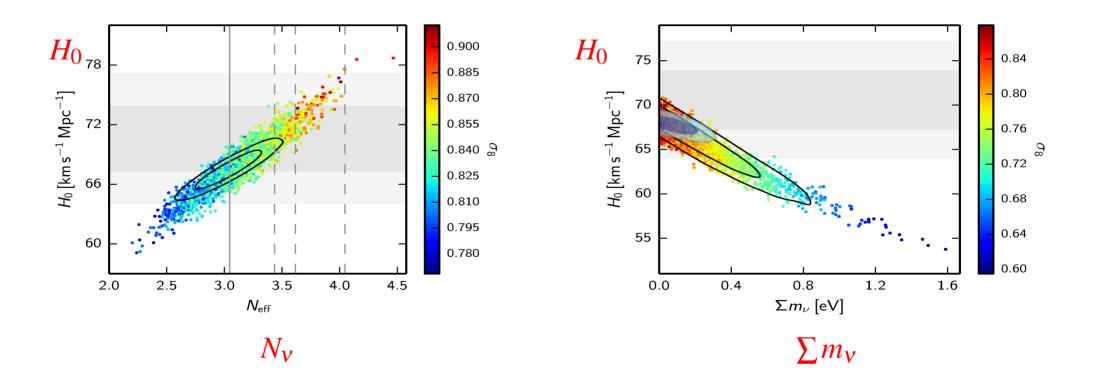
 $\eta_{10} = \eta \cdot 10^{-10} =$ baryon-to-photon ratio. Consistent with CMB determination of η

Neutrino decoupling epoch

Temperature 2-3 MeV, $t\sim 0.1~{\rm s}$

Reactions like $v\bar{v} \leftrightarrow e^+e^-$ switch off. \implies There are 110 cm⁻³ neutrinos of every type today. They are "seen" in properties of CMB, structures.

 $N_{\nu} \approx 3$ in agreement with particle physics. $\sum m_{\nu} \lesssim 0.3$ eV

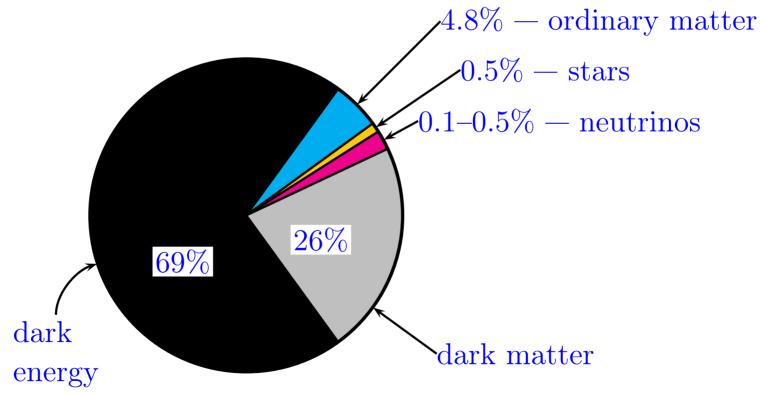


We understand the Universe at age ~ 0.1 s, at temperature ~ 2-3 MeV.
 In particular, gravity was described by General Relativity at

that time.

Yet unknown epochs:

- Generation of dark matter
- Generation of matter-antimatter asymmetry



Present composition of the Universe

$$\Omega_i = rac{
ho_{i,0}}{
ho_c}$$

present fractional energy density of *i*-th type of matter.

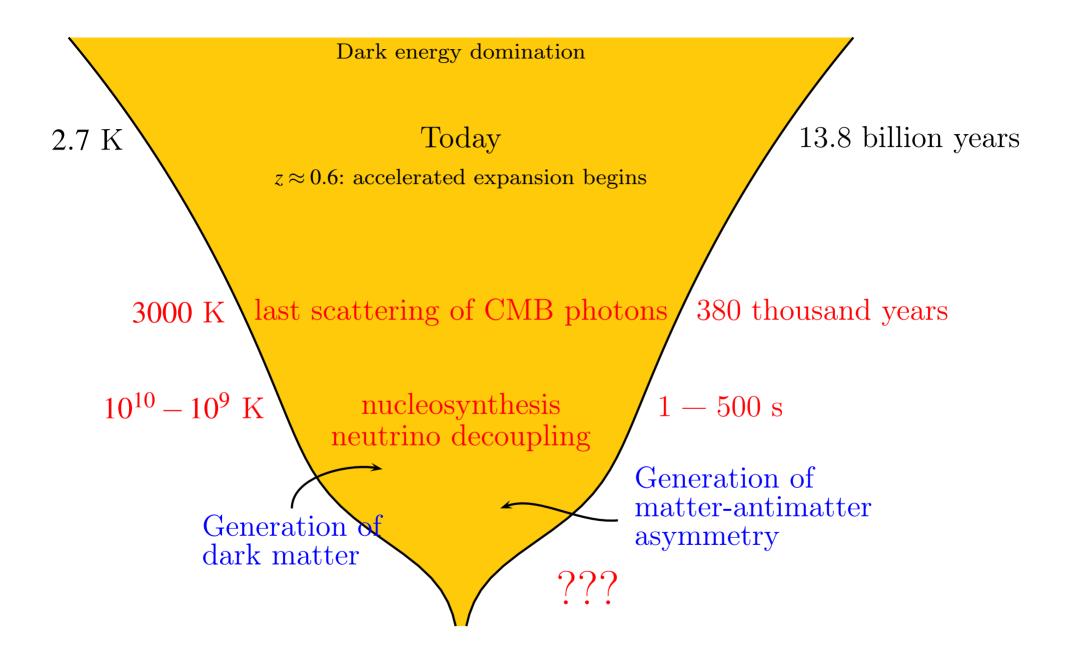
$$\sum_{i} \Omega_i = 1$$

$$\rho_{rad} = \omega(t)n(t)$$
 scales as $\left(\frac{a_0}{a(t)}\right)^4$, since $\omega \propto a^{-1}$.

Friedmann equation

$$H^{2}(t) = \frac{8\pi}{3M_{Pl}^{2}} \left[\rho_{\Lambda} + \rho_{M}(t) + \rho_{rad}(t) \right] = H_{0}^{2} \left[\Omega_{\Lambda} + \Omega_{M} \left(\frac{a_{0}}{a(t)} \right)^{3} + \Omega_{rad} \left(\frac{a_{0}}{a(t)} \right)^{4} \right]$$

 $\begin{array}{l} \ldots \Longrightarrow \mbox{Radiation domination} \Longrightarrow \mbox{Matter domination} \Longrightarrow \mbox{\Lambda-domination} \\ z_{eq} = 3500 & \mbox{now} \\ T_{eq} = 9500 \ \mbox{K} = 0.8 \ \mbox{eV} \\ t_{eq} = 52 \cdot 10^3 \ \mbox{yrs} \end{array}$



With Big Bang nucleosynthesis theory and observations we are confident of the theory of the early Universe at temperatures up to $T \simeq 3$ MeV, age $t \simeq 0.1$ second

With the Large Hadron Collider, we hope to be able to go up to temperatures $T \sim 100$ GeV, age $t \sim 10^{-10}$ second

Are we going to have a handle on even earlier epoch?

Key: cosmological perturbations

Our Universe is not exactly homogeneous.

Inhomogeneities: • density perturbations and associated gravitational potentials (3d scalar), observed;
• gravitational waves (3d tensor), not observed

Today: inhomogeneities strong and non-linear

In the past: amplitudes small,

$$\frac{\delta\rho}{\rho} = 10^{-4} - 10^{-5}$$

Linear analysis appropriate. Go to Fourier space, consider each Fourier mode separately.

Wealth of data

- Cosmic microwave background: photographic picture of the Universe at age 380 000 yrs, T = 3000 K
 - Temperature anisotropy
 - Polarization
- Deep surveys of galaxies and quasars
- Gravitational lensing, etc.

We have already learned a number of fundamental things

Extrapolation back in time with known laws of physics and known elementary particles and fields \implies hot Universe, starts from Big Bang singularity (infinite temperature, infinite expansion rate)

We now know that this is not the whole story.

Key point: causality

Friedmann-Lemaitre-Robertson-Walker metric:

 $ds^2 = dt^2 - a^2(t)d\vec{x}^2$

Expanding Universe:

$$\left(\frac{\dot{a}}{a}\right)^2 \equiv H^2 = \frac{8\pi}{3}G\rho$$

Domination of non-relativistic matter (until recently): $\rho \propto a^{-3} \Longrightarrow a(t) \propto t^{2/3}$

"Radiation domination epoch", before $T\simeq 1$ eV, $t\simeq 50~000~$ years: $\rho\propto a^{-4}\Longrightarrow a(t)\propto t^{1/2}$

Cosmological horizon

length that light travels from Big Bang moment

 $ds^2 = 0 \implies a(t)dx = dt \implies x_H(t) \equiv \eta = \int_0^t \frac{dt'}{a(t')}$, conformal time

 $x_H(t)$: <u>coordinate</u> size of horizon. Physical size at time t:

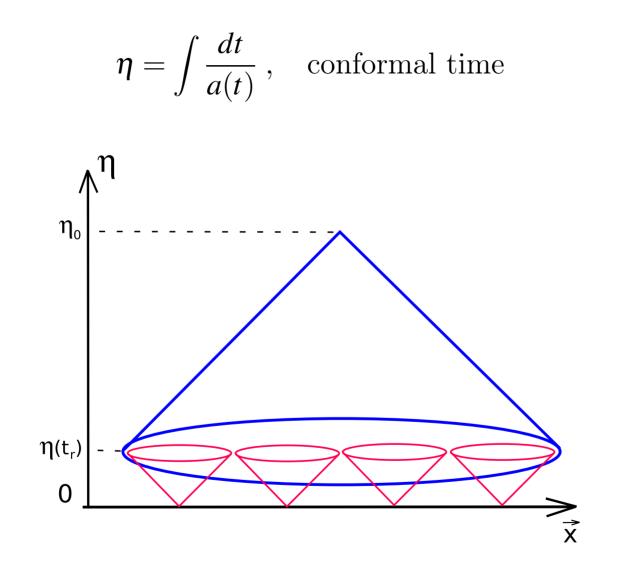
 $l_H(t) = a(t)x_H(t)$

Assume no epoch befor the Hot Big Bang:

integral convergent at low limit $(a \propto t^{1/2}) \Longrightarrow$

$$l_H(t) = (2-3)t$$
 NB: $c = 1$

Causal structure of space-time in hot Big Bang theory (i.e., assuming that the Universe started right from the hot epoch)



Angular size of horizon at recombination $\approx 2^{\circ}$.

Horizon problem

Today our visible Universe consists of $50^3 \sim 10^5$ regions which were causally disconnected at recombination.

Why are they exacly the same?

May sound as a vague question.

But

Properties of perturbations make it sharp and worse.

Major issue: origin of perturbations

Causality \implies perturbations can be generated only when their wavelengths are smaller than horizon size.

Off-hand possibilities:

Perturbations were generated at the hot cosmological epoch by some causal mechanism.

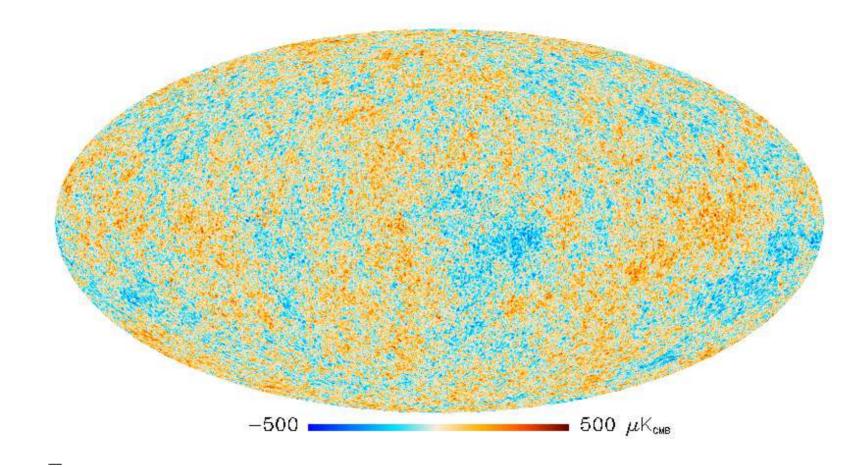
E.g., seeded by topological defects (cosmic strings, etc.)

N. Turok et.al.' 90s

The only possibility, if expansion started from hot Big Bang.

Not an option

Hot epoch was preceded by some other epoch. Perturbations were generated then.



There are perturbations which were superhorizon at the time of recombination, angular scale $\gtrsim 2^{\circ}$. Causality: they could not be generated at hot epoch!

In more detail

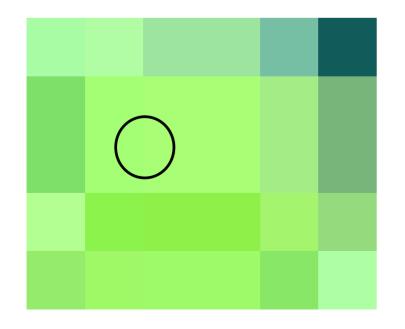
Wavelength of perturbation grows as a(t). E.g., at radiation domination

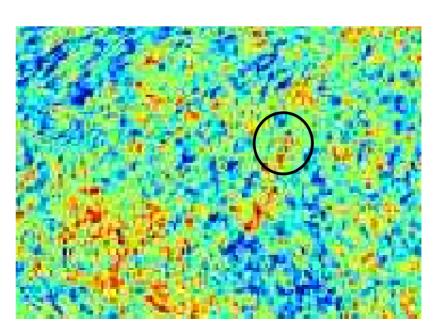
 $\lambda(t) \propto t^{1/2}$ while $l_H \propto t$

Today $\lambda < l_H$, subhorizon regime

Early on $\lambda(t) > l_H$, superhorizon regime.

NB: Horizon entry occured after Big Bang Nucleosynthesis for perturbations of all relevant wavelengths \iff no guesswork.





Shorter wavelengths: perturbations in baryon-photon plasma = sound waves.

If they were superhorizon, they started off with one and the same phase.

Reason: solutions to wave equation in superhorizon regime in expanding Universe

$$\frac{\delta \rho}{\rho} = ext{const}$$
 and $\frac{\delta \rho}{\rho} = \frac{ ext{const}}{t^{3/2}}$

Assume that modes were superhorizon. Consistency of the picture: the Universe was not very inhomogeneous at early times, the initial condition is (up to amplitude),

$$\frac{\delta\rho}{\rho} = \text{const} \implies \frac{d}{dt} \frac{\delta\rho}{\rho} = 0$$

Acoustic oscillations start after entering the horizon at zero velocity of medium \implies phase of oscillations well defined.

Perturbations develop different phases by the time of photon last scattering (= recombination), depending on wave vector:

$$\frac{\delta\rho}{\rho}(t_r) \propto \cos\left(\int_0^{t_r} dt \ v_s \ \frac{k}{a(t)}\right)$$

 $(v_s = \text{sound speed in baryon-photon plasma} \approx 1/\sqrt{3})$ cf. Sakharov oscillations' 1965

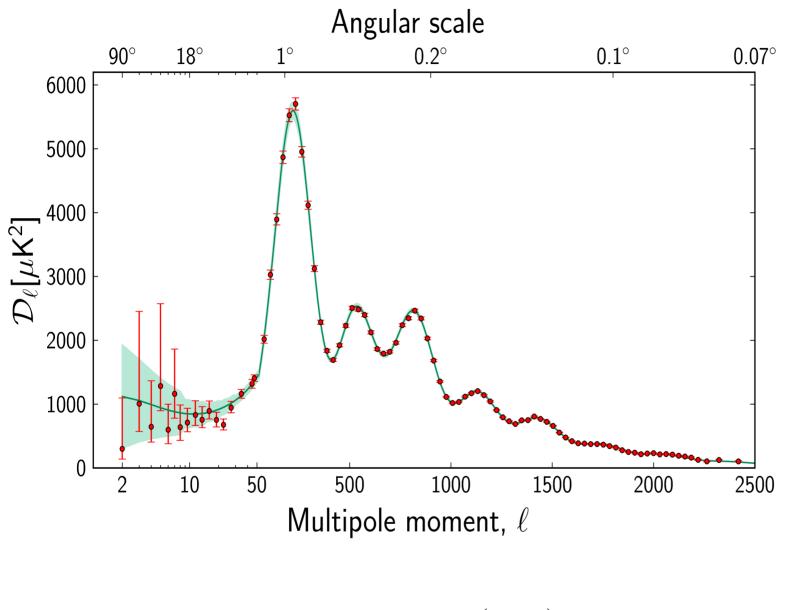
Oscillations in CMB temperature angular spectrum

Fourier decomposition of temperatue fluctuations over celestial sphere:

$$\boldsymbol{\delta T}(\boldsymbol{\theta}, \boldsymbol{\varphi}) = \sum_{l,m} \boldsymbol{a_{lm}} Y_{lm}(\boldsymbol{\theta}, \boldsymbol{\varphi})$$

 $\langle a_{lm}^* a_{lm} \rangle = C_l$, temperature angular spectrum;

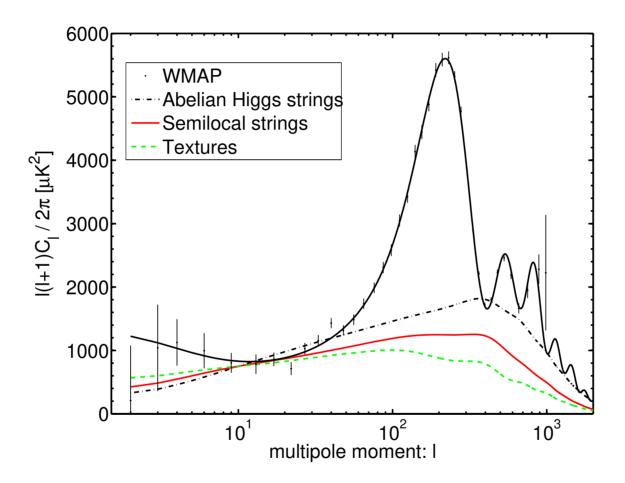
larger $l \iff$ smaller angular scales, shorter wavelengths



Planck

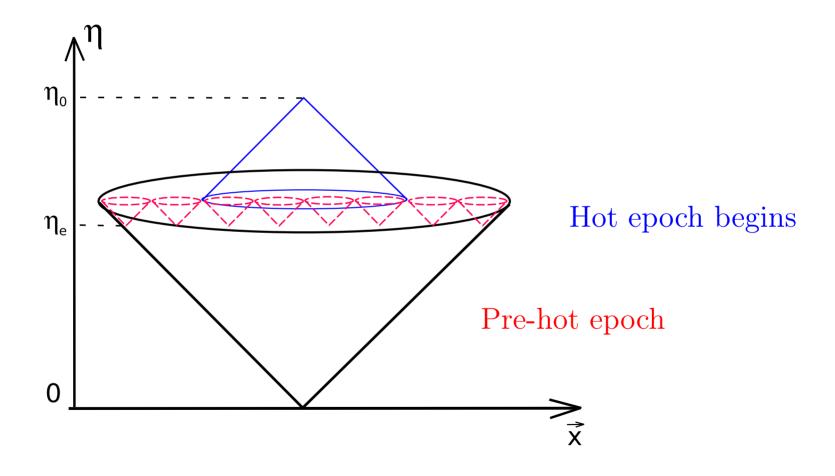
$$\mathscr{D}_l = \frac{l(l+1)}{2\pi} C_l$$

These properties would not be present if perturbations were generated at hot epoch in causal manner.



Primordial perturbations were generated at some yet unknown epoch before the hot expansion stage.

That epoch must have been long (in conformal time) and unusual: perturbations were subhorizon early at that epoch, our visible part of the Universe was in a causally connected region.



Excellent guess: inflation

Starobinsky'79; Guth'81; Linde'82; Albrecht and Steinhardt'82

Exponential expansion with almost constant Hubble rate,

 $a(t) = e^{\int H dt}$, $H \approx const$

$$l_H(t) = a(t) \int_{t_i}^t \frac{dt'}{a(t')} \approx e^{Ht} \int_{t_i}^t e^{-Ht'} dt' \approx e^{H(t-t_i)}$$

- Initially Planck-size region expands to entire visible Universe in $t \sim 100 \ H^{-1} \implies$ for $t \gg 100 \ H^{-1}$ the Universe is VERY large
- Perturbations subhorizon early at inflation:

$$\lambda(t) = 2\pi \frac{a(t)}{k} \ll H^{-1}$$

since $a(t) \propto e^{Ht}$ and $H \approx \text{const}$; wavelengths gets redshifted, the Hubble parameter stays constant

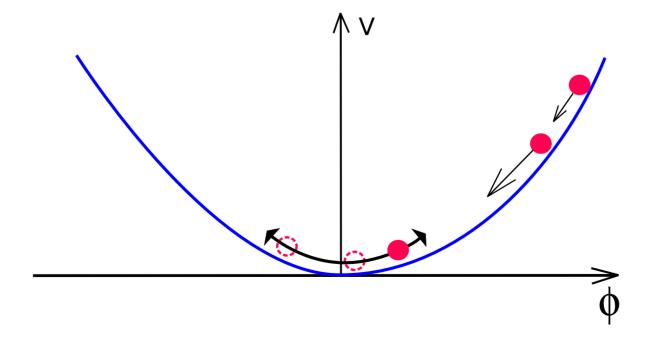
Unusual matter

 $H \approx \text{const} \implies \rho \approx \text{const}$

qualitatively similar to dark energy.

NB: Typical time scale in inflationary models $H^{-1} \sim 10^{-37}$ s energy scale $\rho^{1/4} \simeq \sqrt{M_{Pl}H} \sim 10^{16}$ GeV

Dynamics: slowly rolling scalar field



Alternatives to inflation:

- \blacksquare Bouncing Universe: contraction bounce expansion
- "Genesis": start up from static state

Creminelli et.al.'06; '10

Difficult, but not impossible.

Einstein equations (neglecting spatial curvature)

$$H^{2} = \frac{8\pi}{3}G\rho$$
$$\frac{dH}{dt} = -4\pi(\rho + p)$$

 ρ = energy density, p = effective pressure = $T_{11} = T_{22} = T_{33}$. Bounce, start up scenarios $\Longrightarrow \frac{dH}{dt} > 0 \Longrightarrow \rho > 0$ and $p < -\rho$ Very exotic matter. Potential problems with instabilities, superluminal propagation/causality. Other suggestive observational facts about density perturbations (valid within certain error bars!)

Primordial perturbations are Gaussian.

This suggests the origin: enhanced vacuum fluctuations of weakly coupled quatum field(s)

 Inflation does the job very well: vacuum fluctuations of all light fields get enhanced greatly due to fast expansion of the Universe.

Including the field that dominates energy density (inflaton) \implies perturbations in energy density.

Mukhanov, Chibisov'81; Hawking'82; Starobinsky'82; Guth, Pi'82; Bardeen et.al.'83

 Enhancement of vacuum fluctuations is less automatic in alternative scenarios Primordial power spectrum is almost flat: no length scale Homogeneity and anisotropy of Gaussian random field:

$$\langle \frac{\delta \rho}{\rho}(\vec{k}) \frac{\delta \rho}{\rho}(\vec{k}') \rangle = \frac{1}{4\pi k^3} \mathscr{P}(k) \delta(\vec{k} + \vec{k}')$$

 $\mathscr{P}(k) =$ power spectrum, gives fluctuation in logarithmic interval of momenta,

$$\left\langle \left(\frac{\delta\rho}{\rho}(\vec{x})\right)^2 \right\rangle = \int_0^\infty \frac{dk}{k} \mathscr{P}(k)$$

Flat spectrum: \mathscr{P} is independent of k Harrison' 70; Zeldovich' 72, Peebles, Yu' 70

Parametrization

$$\mathscr{P}(k) = A\left(\frac{k}{k_*}\right)^{n_s - 1}$$

 $\begin{array}{l} A = \text{amplitude, } (n_s - 1) = \text{tilt, } k_* = \text{fiducial momentum (matter of convention). Flat spectrum } \Longleftrightarrow n_s = 1.\\ \text{Experiment: } n_s = 0.965 \pm 0.004 \text{ (WMAP, Planck)} \end{array}$

There must be some symmetry behind flatness of spectrum

■ Inflation: symmetry of de Sitter space-time SO(4,1)

$$ds^2 = dt^2 - e^{2Ht} d\vec{x}^2$$

Relevant symmetry: spatial dilatations supplemented by time translations

$$\vec{x} \to \lambda \vec{x} , \quad t \to t - \frac{1}{2H} \log \lambda$$

• Alternative: conformal symmetry SO(4,2)

Conformal group includes dilatations, $x^{\mu} \rightarrow \lambda x^{\mu}$. \implies No scale, good chance for flatness of spectrum

> First mentioned by Antoniadis, Mazur, Mottola' 97 Concrete models: V.R.' 09; Creminelli, Nicolis, Trincherini' 10.

NB: (Super)conformal symmetry has long been discussed in the context of Quantum Field Theory and particle physics.

Large and powerful symmetry behind, e.g., adS/CFT correspondence and a number of other QFT phenomena

It may well be that ultimate theory of Nature is (super)conformal

What if our Universe started off from or passed through an unstable (super)conformal state and then evolved to much less symmetric state we see today?

Exploratory stage: toy models + general arguments so far.

Can one tell?

More intricate properties of cosmological perturbations Not detected yet.

Primordial gravitational waves predicted by simplest (hence plausible) inflationary models, but not alternatives to inflation

Smoking gun for inflation

Huge wavelengths, sizeable amplitudes, $h \sim 10^{-5} - 10^{-6}$ (cf. $h \leq 10^{-22}$ for gravity waves of astrophysical origin)

Almost flat power spectrum.

 $\begin{array}{ll} \text{Metric perturbations:} & ds^2 = dt^2 - a^2(t)(\delta_{ij} + h_{ij})dx^i dx^j \\ h_{ij} = h_{ij}(\vec{x},t), \ h_i^i = \partial_i h_j^i = 0, \ \text{spin } 2. \end{array}$

Gravity waves: effects on CMB Temperature anisotropy (in addition to effect of scalar perturbations)

V.R., Sazhin, Veryaskin' 1982; Fabbri, Pollock' 83

NB: gravity wave amplitudes are time-independent when superhorizon and decay as $h_{ij} \propto a^{-1}(t)$ in subhorizon regime.

Strongest contribution to δT at large angles

 $\Delta\theta \gtrsim 2^o, \ l \lesssim 50,$ Present wavelengths ~1 Gpc

Polarization

Basko, Polnarev' 1980; Polnarev' 1985; Sazhin, Benitez' 1995

especially B-mode

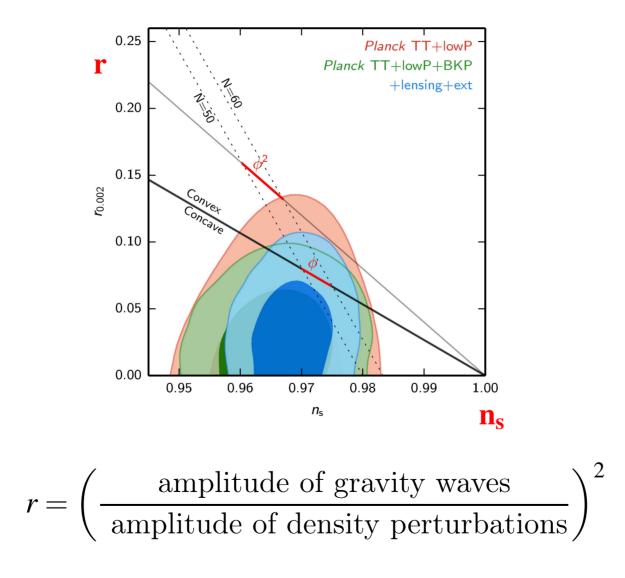
Kamionkowski, Kosowski, Stebbins' 1997; Seljak, Zaldarriaga' 1997 Weak signal, degree of polarization $P(l) \propto l$ at $l \lesssim 50$ and decays with l at l > 50.

Amplitude (at r = 0.2):

 $P(l \sim 30) \sim 3 \cdot 10^{-8} \Longrightarrow P \cdot T \sim 0.1 \ \mu \text{K}$

Present situation

Scalar spectral index vs gravity waves



BICEP-2 claim (March 2014): $r \approx 0.2$ not confirmed

Non-Gaussianity: big issue

- Very small in the simplest inflationary theories
- Sizeable in more contrived inflationary models and in alternatives to inflation. Often begins with bispectrum

$$\langle \frac{\delta\rho}{\rho}(\mathbf{k}_1) \frac{\delta\rho}{\rho}(\mathbf{k}_2) \frac{\delta\rho}{\rho}(\mathbf{k}_3) \rangle = \delta(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) G(k_i^2, \mathbf{k}_1 \mathbf{k}_2, \mathbf{k}_1 \mathbf{k}_3)$$

Shape of $G(k_i^2, \mathbf{k_1 k_2}, \mathbf{k_1 k_3})$ different in different models \Longrightarrow potential discriminator.

Statistical anisotropy

$$\mathscr{P}(\mathbf{k}) = \mathscr{P}_0(k) \left(1 + w_{ij}(k) \frac{k_i k_j}{k^2} + \dots \right)$$

- Anisotropy of the Universe at pre-hot stage
- Possible in inflation with strong vector fields (rather contrived)

Ackerman, Carroll, Wise' 07; Pullen, Kamionkowski' 07; Watanabe, Kanno, Soda' 09

• Natural in conformal models

Libanov, V.R.' 10; Libanov, Ramazanov, V.R.' 11

Entropy perturbations

Adiabatic perturbations:

Perturbations in energy densioty but not in composition

 $\frac{\text{dark matter density}}{\text{entropy density}} = \text{const in space}$

Likewise for usual matter.

The only option if dark matter and/or matter-antimatter asymmetry were generated at hot epoch.

Entropy perturbations = perturbations in composition

No admixture of entropy perturbations detected; strong limits from Planck.

To summarize:

- No doubt there was an epoch preceding the hot Big Bang. The question is what was that epoch?
- Inflation is consistent with all data. But there are competitors: the data may rather point towards (super)conformal beginning of the cosmological evolution.

More options:

Matter bounce, Finelli, Brandenberger' 01.

Negative exponential potential, Lehners et. al.' 07; Buchbinder, Khouri, Ovrut' 07; Creminelli, Senatore' 07.

Lifshitz scalar, Mukohyama' 09

- Only very basic things are known for the time being.
- To tell, we need to discover

more intricate properties of cosmological perturbations

\checkmark Primordial tensor modes = gravitational waves

Sizeable amplitude, (almost) flat power spectrum predicted by simplest (and hence most plausible) inflationary models but not alternatives to inflation

- Together with scalar and tensor tilts \implies properties of inflation
- Non-trivial correlation properties of density perturbations (non-Gaussianity) => potential discriminator between scenarios. Very small in single field inflation.
 - Shape of non-Gaussianity: function of invariants $(\vec{k}_1 \cdot \vec{k}_2)$, etc.
- - Shape of statistical anisotropy \implies specific anisotropic model
- Admixture of entropy perturbations ⇒ generation of dark matter and/or matter-antimatter asymmetry before the hot epoch.

At the eve of new physics

chance to learn what preceded the hot Big Bang epoch

Barring the possibility that Nature is dull



BICEP-2 saga

Power spectra of tensor (gravity waves) and scalar perturbations (per log interval of momenta=wave numbers)

$$\mathscr{P}_T = \frac{16}{\pi} \frac{H_{infl}^2}{M_{Pl}^2} = \frac{128}{3} \frac{\rho_{infl}}{M_{Pl}^4} , \quad \mathscr{P}_s = 2.5 \cdot 10^{-9}$$

Notation: tensor-to-scalar ratio

$$r = \frac{\mathscr{P}_T}{\mathscr{P}_s}$$

Scalar spectral index

$$\mathscr{P}_{s}(k) = \mathscr{P}_{s}(k_{*}) \cdot \left(\frac{k}{k_{*}}\right)^{n_{s}-1}$$

Predictions of inflationary models

Assume power-law inflaton potential $V(\phi) = g\phi^n$. Then

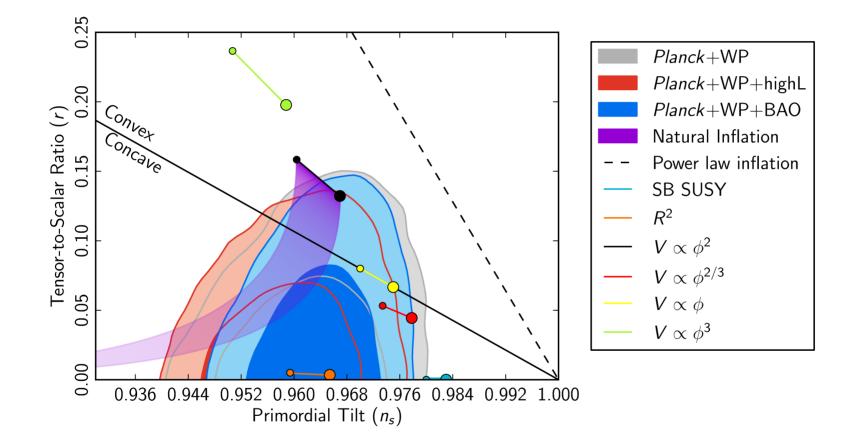
$$r = \frac{4n}{N_e} \qquad n_s - 1 = -\frac{n+2}{2N_e}$$
$$N_e = \ln \frac{a_e}{a_{\times}} = 50 - 60$$

 $a_e =$ scale factor at the end of inflation

 a_{\times} = scale factor at the time when our visible Universe exits the horizon at inflation.

Planck-2013 + everybody else

Scalar spectral index vs. power of tensors

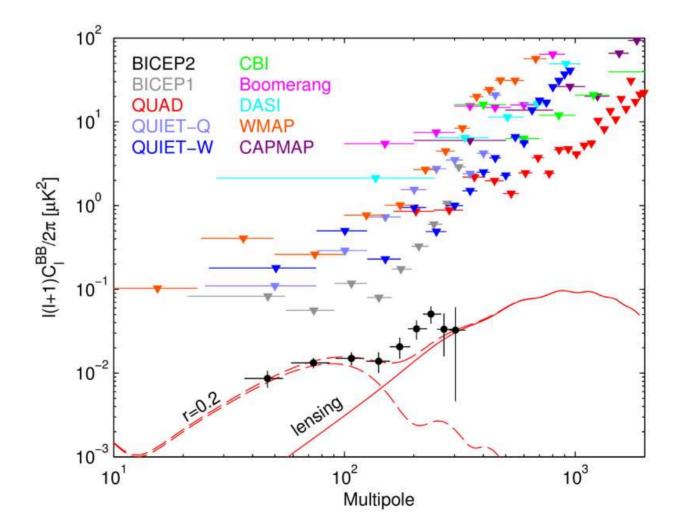


BICEP-2 at South pole

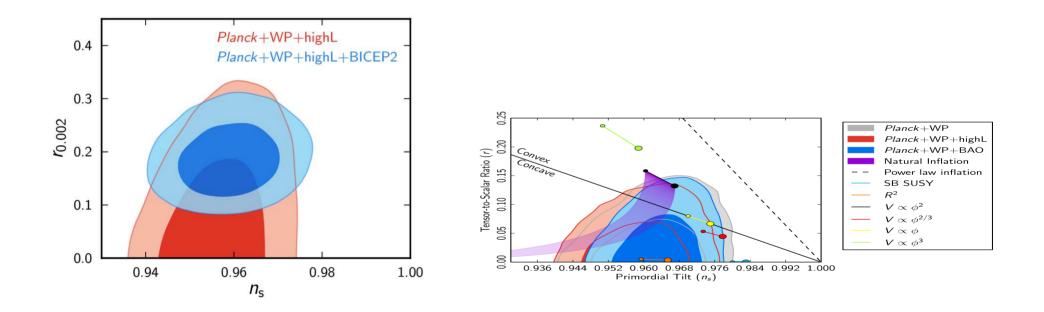
- 590 days of data taking
- Sky region of 390 square degrees towards Galactic pole
- One frequency 150 GHz
- March 2013: claim of discovery of CMB polarization generated by relic gravity waves

BICEP-2 result

9 30 < l < 150, $r = 0.2^{+0.07}_{-0.05}$, $r \neq 0 > 5\sigma$



Tension between BICEP-2 and Planck:



BICEP-2 and Planck with $\frac{dn_s}{d} \ln k = -0.02$ (very large!) Inflation: $\frac{dn_s}{d} \ln k \approx -0.001$ Planck + others

Were this the discovery, then

Proof of inflation

•
$$\rho_{infl}^{1/4} = 2 \cdot 10^{16} \text{ GeV}$$

 Experimental proof of linearized quantum gravity (no wonder!)

In future:

Tensor spectral index \implies consistency relation in single field inflation

$$n_T = -\frac{r}{8}$$

Signal is there.

Are there relic gravity waves???

Dangerous "foreground": polarized dust in our Galaxy, $r\sim 0.1~\mu{\rm m}$

Oriented by Galactic magnetic field, emits polarized radiation (way to study magnetic fields in our Galaxy)

Dominates completely at high frequencies

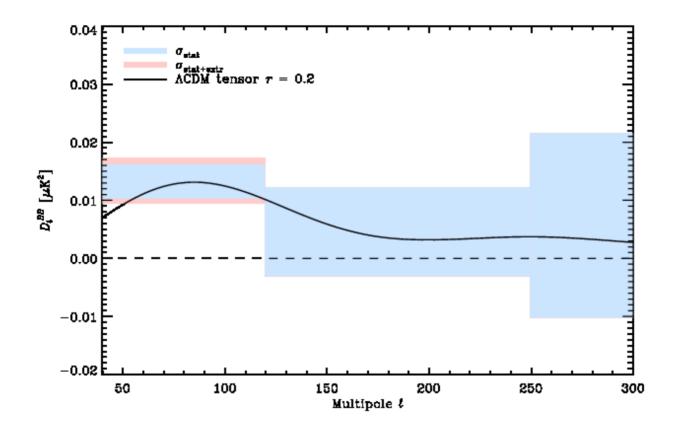
Poorly known until very recently

Prejudice: negligible at Galactic polar regions.

And what's the reality?

Planck, September 2014: analyzed dust contribution to polarization

Planck-2014



Extrapolation of dust contribution from 353 GHz to 150 GHz (shaded regions)

Solid line: expected gravity wave signal at r = 0.2

NB: Same patch of the sky as used by BICEP-2

Smells like dust, looks like dust, tastes like dust...

Discovery postponed – too bad!

Hard task for experimentalists: extract signal from relic gravity waves from dust foreground

Especially if r < 0.1